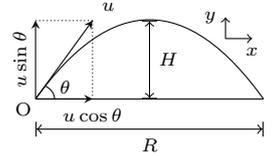


PHYSICS FORMULA LIST

0.1: Physical Constants

Speed of light	c	$3 \times 10^8 \text{ m/s}$
Planck constant	h	$6.63 \times 10^{-34} \text{ J s}$
	hc	1242 eV-nm
Gravitation constant	G	$6.67 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$
Boltzmann constant	k	$1.38 \times 10^{-23} \text{ J/K}$
Molar gas constant	R	8.314 J/(mol K)
Avogadro's number	N_A	$6.023 \times 10^{23} \text{ mol}^{-1}$
Charge of electron	e	$1.602 \times 10^{-19} \text{ C}$
Permeability of vacuum	μ_0	$4\pi \times 10^{-7} \text{ N/A}^2$
Permittivity of vacuum	ϵ_0	$8.85 \times 10^{-12} \text{ F/m}$
Coulomb constant	$\frac{1}{4\pi\epsilon_0}$	$9 \times 10^9 \text{ N m}^2/\text{C}^2$
Faraday constant	F	96485 C/mol
Mass of electron	m_e	$9.1 \times 10^{-31} \text{ kg}$
Mass of proton	m_p	$1.6726 \times 10^{-27} \text{ kg}$
Mass of neutron	m_n	$1.6749 \times 10^{-27} \text{ kg}$
Atomic mass unit	u	$1.66 \times 10^{-27} \text{ kg}$
Atomic mass unit	u	$931.49 \text{ MeV}/c^2$
Stefan-Boltzmann constant	σ	$5.67 \times 10^{-8} \text{ W}/(\text{m}^2 \text{ K}^4)$
Rydberg constant	R_∞	$1.097 \times 10^7 \text{ m}^{-1}$
Bohr magneton	μ_B	$9.27 \times 10^{-24} \text{ J/T}$
Bohr radius	a_0	$0.529 \times 10^{-10} \text{ m}$
Standard atmosphere	atm	$1.01325 \times 10^5 \text{ Pa}$
Wien displacement constant	b	$2.9 \times 10^{-3} \text{ m K}$



Projectile Motion:

$$x = ut \cos \theta, \quad y = ut \sin \theta - \frac{1}{2}gt^2$$

$$y = x \tan \theta - \frac{g}{2u^2 \cos^2 \theta} x^2$$

$$T = \frac{2u \sin \theta}{g}, \quad R = \frac{u^2 \sin 2\theta}{g}, \quad H = \frac{u^2 \sin^2 \theta}{2g}$$

1.3: Newton's Laws and Friction

Linear momentum: $\vec{p} = m\vec{v}$

Newton's first law: inertial frame.

Newton's second law: $\vec{F} = \frac{d\vec{p}}{dt}$, $\vec{F} = m\vec{a}$

Newton's third law: $\vec{F}_{AB} = -\vec{F}_{BA}$

Frictional force: $f_{\text{static, max}} = \mu_s N$, $f_{\text{kinetic}} = \mu_k N$

Banking angle: $\frac{v^2}{rg} = \tan \theta$, $\frac{v^2}{rg} = \frac{\mu + \tan \theta}{1 - \mu \tan \theta}$

Centripetal force: $F_c = \frac{mv^2}{r}$, $a_c = \frac{v^2}{r}$

Pseudo force: $\vec{F}_{\text{pseudo}} = -m\vec{a}_0$, $F_{\text{centrifugal}} = -\frac{mv^2}{r}$

Minimum speed to complete vertical circle:

$$v_{\text{min, bottom}} = \sqrt{5gl}, \quad v_{\text{min, top}} = \sqrt{gl}$$

MECHANICS

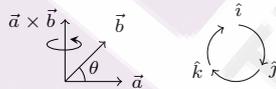
1.1: Vectors

Notation: $\vec{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k}$

Magnitude: $a = |\vec{a}| = \sqrt{a_x^2 + a_y^2 + a_z^2}$

Dot product: $\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z = ab \cos \theta$

Cross product:



$$\vec{a} \times \vec{b} = (a_y b_z - a_z b_y) \hat{i} + (a_z b_x - a_x b_z) \hat{j} + (a_x b_y - a_y b_x) \hat{k}$$

$$|\vec{a} \times \vec{b}| = ab \sin \theta$$

1.2: Kinematics

Average and Instantaneous Vel. and Accel.:

$$\vec{v}_{\text{av}} = \Delta \vec{r} / \Delta t, \quad \vec{v}_{\text{inst}} = d\vec{r} / dt$$

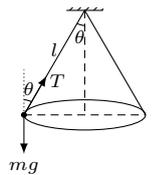
$$\vec{a}_{\text{av}} = \Delta \vec{v} / \Delta t, \quad \vec{a}_{\text{inst}} = d\vec{v} / dt$$

Motion in a straight line with constant a :

$$v = u + at, \quad s = ut + \frac{1}{2}at^2, \quad v^2 - u^2 = 2as$$

Relative Velocity: $\vec{v}_{A/B} = \vec{v}_A - \vec{v}_B$

Conical pendulum: $T = 2\pi \sqrt{\frac{l \cos \theta}{g}}$



1.4: Work, Power and Energy

Work: $W = \vec{F} \cdot \vec{S} = FS \cos \theta$, $W = \int \vec{F} \cdot d\vec{S}$

Kinetic energy: $K = \frac{1}{2}mv^2 = \frac{p^2}{2m}$

Potential energy: $F = -\partial U / \partial x$ for conservative forces.

$$U_{\text{gravitational}} = mgh, \quad U_{\text{spring}} = \frac{1}{2}kx^2$$

Work done by conservative forces is path independent and depends only on initial and final points:
 $\oint \vec{F}_{\text{conservative}} \cdot d\vec{r} = 0$.

Work-energy theorem: $W = \Delta K$

Mechanical energy: $E = U + K$. Conserved if forces are conservative in nature.

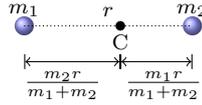
Power $P_{\text{av}} = \frac{\Delta W}{\Delta t}$, $P_{\text{inst}} = \vec{F} \cdot \vec{v}$

1.5: Centre of Mass and Collision

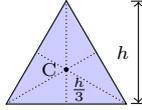
Centre of mass: $x_{cm} = \frac{\sum x_i m_i}{\sum m_i}$, $x_{cm} = \frac{\int x dm}{\int dm}$

CM of few useful configurations:

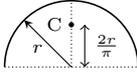
1. m_1, m_2 separated by r :



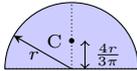
2. Triangle (CM \equiv Centroid) $y_c = \frac{h}{3}$



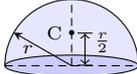
3. Semicircular ring: $y_c = \frac{2r}{\pi}$



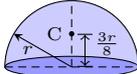
4. Semicircular disc: $y_c = \frac{4r}{3\pi}$



5. Hemispherical shell: $y_c = \frac{r}{2}$



6. Solid Hemisphere: $y_c = \frac{3r}{8}$



7. Cone: the height of CM from the base is $h/4$ for the solid cone and $h/3$ for the hollow cone.

Motion of the CM: $M = \sum m_i$

$$\vec{v}_{cm} = \frac{\sum m_i \vec{v}_i}{M}, \quad \vec{p}_{cm} = M \vec{v}_{cm}, \quad \vec{a}_{cm} = \frac{\vec{F}_{ext}}{M}$$

Impulse: $\vec{J} = \int \vec{F} dt = \Delta \vec{p}$

Collision:



Momentum conservation: $m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$

Elastic Collision: $\frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 = \frac{1}{2} m_1 v_1'^2 + \frac{1}{2} m_2 v_2'^2$

Coefficient of restitution:

$$e = \frac{-(v_1' - v_2')}{v_1 - v_2} = \begin{cases} 1, & \text{completely elastic} \\ 0, & \text{completely in-elastic} \end{cases}$$

If $v_2 = 0$ and $m_1 \ll m_2$ then $v_1' = -v_1$.

If $v_2 = 0$ and $m_1 \gg m_2$ then $v_2' = 2v_1$.

Elastic collision with $m_1 = m_2$: $v_1' = v_2$ and $v_2' = v_1$.

1.6: Rigid Body Dynamics

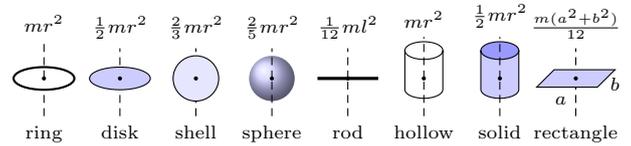
Angular velocity: $\omega_{av} = \frac{\Delta \theta}{\Delta t}$, $\omega = \frac{d\theta}{dt}$, $\vec{v} = \vec{\omega} \times \vec{r}$

Angular Accel.: $\alpha_{av} = \frac{\Delta \omega}{\Delta t}$, $\alpha = \frac{d\omega}{dt}$, $\vec{a} = \vec{\alpha} \times \vec{r}$

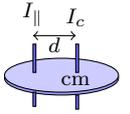
Rotation about an axis with constant α :

$$\omega = \omega_0 + \alpha t, \quad \theta = \omega t + \frac{1}{2} \alpha t^2, \quad \omega^2 - \omega_0^2 = 2\alpha \theta$$

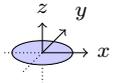
Moment of Inertia: $I = \sum_i m_i r_i^2$, $I = \int r^2 dm$



Theorem of Parallel Axes: $I_{||} = I_{cm} + md^2$



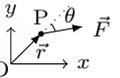
Theorem of Perp. Axes: $I_z = I_x + I_y$



Radius of Gyration: $k = \sqrt{I/m}$

Angular Momentum: $\vec{L} = \vec{r} \times \vec{p}$, $\vec{L} = I\vec{\omega}$

Torque: $\vec{\tau} = \vec{r} \times \vec{F}$, $\vec{\tau} = \frac{d\vec{L}}{dt}$, $\tau = I\alpha$



Conservation of \vec{L} : $\vec{\tau}_{ext} = 0 \implies \vec{L} = \text{const.}$

Equilibrium condition: $\sum \vec{F} = \vec{0}$, $\sum \vec{\tau} = \vec{0}$

Kinetic Energy: $K_{rot} = \frac{1}{2} I \omega^2$

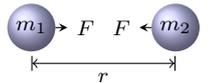
Dynamics:

$$\vec{\tau}_{cm} = I_{cm} \vec{\alpha}, \quad \vec{F}_{ext} = m \vec{a}_{cm}, \quad \vec{p}_{cm} = m \vec{v}_{cm}$$

$$K = \frac{1}{2} m v_{cm}^2 + \frac{1}{2} I_{cm} \omega^2, \quad \vec{L} = I_{cm} \vec{\omega} + \vec{r}_{cm} \times m \vec{v}_{cm}$$

1.7: Gravitation

Gravitational force: $F = G \frac{m_1 m_2}{r^2}$



Potential energy: $U = -\frac{GMm}{r}$

Gravitational acceleration: $g = \frac{GM}{R^2}$

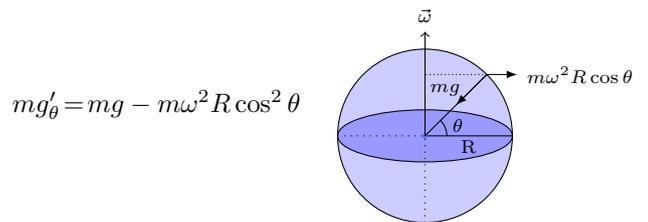
Variation of g with depth: $g_{inside} \approx g \left(1 - \frac{2h}{R}\right)$

Variation of g with height: $g_{outside} \approx g \left(1 - \frac{h}{R}\right)$

Effect of non-spherical earth shape on g :

$$g_{at \text{ pole}} > g_{at \text{ equator}} \quad (\because R_e - R_p \approx 21 \text{ km})$$

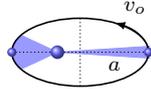
Effect of earth rotation on apparent weight:



Orbital velocity of satellite: $v_o = \sqrt{\frac{GM}{R}}$

Escape velocity: $v_e = \sqrt{\frac{2GM}{R}}$

Kepler's laws:



- First:** Elliptical orbit with sun at one of the focus.
- Second:** Areal velocity is constant. ($\therefore d\vec{L}/dt = 0$).
- Third:** $T^2 \propto a^3$. In circular orbit $T^2 = \frac{4\pi^2}{GM} a^3$.

1.8: Simple Harmonic Motion

Hooke's law: $F = -kx$ (for small elongation x .)

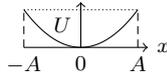
Acceleration: $a = \frac{d^2x}{dt^2} = -\frac{k}{m}x = -\omega^2x$

Time period: $T = \frac{2\pi}{\omega} = 2\pi\sqrt{\frac{m}{k}}$

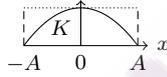
Displacement: $x = A \sin(\omega t + \phi)$

Velocity: $v = A\omega \cos(\omega t + \phi) = \pm\omega\sqrt{A^2 - x^2}$

Potential energy: $U = \frac{1}{2}kx^2$

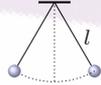


Kinetic energy $K = \frac{1}{2}mv^2$



Total energy: $E = U + K = \frac{1}{2}m\omega^2A^2$

Simple pendulum: $T = 2\pi\sqrt{\frac{l}{g}}$



Physical Pendulum: $T = 2\pi\sqrt{\frac{I}{mgl}}$



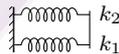
Torsional Pendulum $T = 2\pi\sqrt{\frac{I}{k}}$



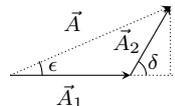
Springs in series: $\frac{1}{k_{eq}} = \frac{1}{k_1} + \frac{1}{k_2}$



Springs in parallel: $k_{eq} = k_1 + k_2$



Superposition of two SHM's:



$$x_1 = A_1 \sin \omega t, \quad x_2 = A_2 \sin(\omega t + \delta)$$

$$x = x_1 + x_2 = A \sin(\omega t + \epsilon)$$

$$A = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos \delta}$$

$$\tan \epsilon = \frac{A_2 \sin \delta}{A_1 + A_2 \cos \delta}$$

1.9: Properties of Matter

Modulus of rigidity: $Y = \frac{F/A}{\Delta l/l}, B = -V \frac{\Delta P}{\Delta V}, \eta = \frac{F}{A\theta}$

Compressibility: $K = \frac{1}{B} = -\frac{1}{V} \frac{dV}{dP}$

Poisson's ratio: $\sigma = \frac{\text{lateral strain}}{\text{longitudinal strain}} = \frac{\Delta D/D}{\Delta l/l}$

Elastic energy: $U = \frac{1}{2} \text{stress} \times \text{strain} \times \text{volume}$

Surface tension: $S = F/l$

Surface energy: $U = SA$

Excess pressure in bubble:

$$\Delta p_{\text{air}} = 2S/R, \quad \Delta p_{\text{soap}} = 4S/R$$

Capillary rise: $h = \frac{2S \cos \theta}{r\rho g}$

Hydrostatic pressure: $p = \rho gh$

Buoyant force: $F_B = \rho V g = \text{Weight of displaced liquid}$

Equation of continuity: $A_1v_1 = A_2v_2$ 

Bernoulli's equation: $p + \frac{1}{2}\rho v^2 + \rho gh = \text{constant}$

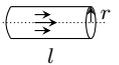
Torricelli's theorem: $v_{\text{efflux}} = \sqrt{2gh}$

Viscous force: $F = -\eta A \frac{dv}{dx}$

Stoke's law: $F = 6\pi\eta r v$



Poiseuille's equation: $\frac{\text{Volume flow}}{\text{time}} = \frac{\pi pr^4}{8\eta l}$



Terminal velocity: $v_t = \frac{2r^2(\rho - \sigma)g}{9\eta}$

Waves

2.1: Waves Motion

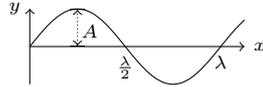
General equation of wave: $\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}$.

Notation: Amplitude A , Frequency ν , Wavelength λ , Period T , Angular Frequency ω , Wave Number k ,

$$T = \frac{1}{\nu} = \frac{2\pi}{\omega}, \quad v = \nu\lambda, \quad k = \frac{2\pi}{\lambda}$$

Progressive wave travelling with speed v :

$$y = f(t - x/v), \rightsquigarrow +x; \quad y = f(t + x/v), \rightsquigarrow -x$$



Progressive sine wave:

$$y = A \sin(kx - \omega t) = A \sin(2\pi(x/\lambda - t/T))$$

2.2: Waves on a String

Speed of waves on a string with mass per unit length μ and tension T : $v = \sqrt{T/\mu}$

Transmitted power: $P_{av} = 2\pi^2 \mu v A^2 \nu^2$

Interference:

$$y_1 = A_1 \sin(kx - \omega t), \quad y_2 = A_2 \sin(kx - \omega t + \delta)$$

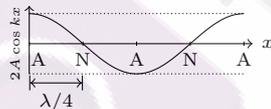
$$y = y_1 + y_2 = A \sin(kx - \omega t + \epsilon)$$

$$A = \sqrt{A_1^2 + A_2^2 + 2A_1 A_2 \cos \delta}$$

$$\tan \epsilon = \frac{A_2 \sin \delta}{A_1 + A_2 \cos \delta}$$

$$\delta = \begin{cases} 2n\pi, & \text{constructive;} \\ (2n+1)\pi, & \text{destructive.} \end{cases}$$

Standing Waves:

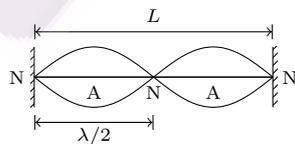


$$y_1 = A_1 \sin(kx - \omega t), \quad y_2 = A_2 \sin(kx + \omega t)$$

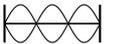
$$y = y_1 + y_2 = (2A \cos kx) \sin \omega t$$

$$x = \begin{cases} (n + \frac{1}{2}) \frac{\lambda}{2}, & \text{nodes; } n = 0, 1, 2, \dots \\ n \frac{\lambda}{2}, & \text{antinodes. } n = 0, 1, 2, \dots \end{cases}$$

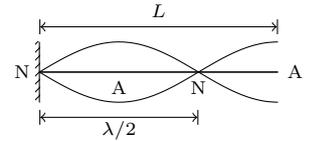
String fixed at both ends:



- Boundary conditions: $y = 0$ at $x = 0$ and at $x = L$
- Allowed Freq.: $L = n \frac{\lambda}{2}$, $\nu = \frac{n}{2L} \sqrt{\frac{T}{\mu}}$, $n = 1, 2, 3, \dots$
- Fundamental/1st harmonics: $\nu_0 = \frac{1}{2L} \sqrt{\frac{T}{\mu}}$ 

- 1st overtone/2nd harmonics: $\nu_1 = \frac{2}{2L} \sqrt{\frac{T}{\mu}}$ 
- 2nd overtone/3rd harmonics: $\nu_2 = \frac{3}{2L} \sqrt{\frac{T}{\mu}}$ 
- All harmonics are present.

String fixed at one end:



- Boundary conditions: $y = 0$ at $x = 0$
- Allowed Freq.: $L = (2n + 1) \frac{\lambda}{4}$, $\nu = \frac{2n+1}{4L} \sqrt{\frac{T}{\mu}}$, $n = 0, 1, 2, \dots$
- Fundamental/1st harmonics: $\nu_0 = \frac{1}{4L} \sqrt{\frac{T}{\mu}}$ 
- 1st overtone/3rd harmonics: $\nu_1 = \frac{3}{4L} \sqrt{\frac{T}{\mu}}$ 
- 2nd overtone/5th harmonics: $\nu_2 = \frac{5}{4L} \sqrt{\frac{T}{\mu}}$ 
- Only odd harmonics are present.

Sonometer: $\nu \propto \frac{1}{L}$, $\nu \propto \sqrt{T}$, $\nu \propto \frac{1}{\sqrt{\mu}}$, $\nu = \frac{n}{2L} \sqrt{\frac{T}{\mu}}$

2.3: Sound Waves

Displacement wave: $s = s_0 \sin \omega(t - x/v)$

Pressure wave: $p = p_0 \cos \omega(t - x/v)$, $p_0 = (B\omega/v)s_0$

Speed of sound waves:

$$v_{\text{liquid}} = \sqrt{\frac{B}{\rho}}, \quad v_{\text{solid}} = \sqrt{\frac{Y}{\rho}}, \quad v_{\text{gas}} = \sqrt{\frac{\gamma P}{\rho}}$$

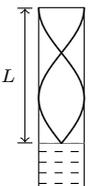
Intensity: $I = \frac{2\pi^2 B}{v} s_0^2 \nu^2 = \frac{p_0^2 v}{2B} = \frac{p_0^2}{2\rho v}$

Standing longitudinal waves:

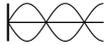
$$p_1 = p_0 \sin \omega(t - x/v), \quad p_2 = p_0 \sin \omega(t + x/v)$$

$$p = p_1 + p_2 = 2p_0 \cos kx \sin \omega t$$

Closed organ pipe:



- Boundary condition: $y = 0$ at $x = 0$
- Allowed freq.: $L = (2n + 1) \frac{\lambda}{4}$, $\nu = (2n + 1) \frac{v}{4L}$, $n = 0, 1, 2, \dots$
- Fundamental/1st harmonics: $\nu_0 = \frac{v}{4L}$ 
- 1st overtone/3rd harmonics: $\nu_1 = 3\nu_0 = \frac{3v}{4L}$ 

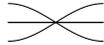
5. 2nd overtone/5th harmonics: $\nu_2 = 5\nu_0 = \frac{5v}{4L}$ 

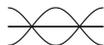
6. Only odd harmonics are present.

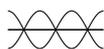
Open organ pipe:



1. Boundary condition: $y = 0$ at $x = 0$
Allowed freq.: $L = n\frac{\lambda}{2}$, $\nu = n\frac{v}{4L}$, $n = 1, 2, \dots$

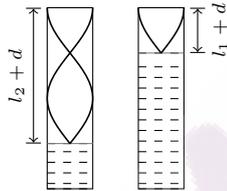
2. Fundamental/1st harmonics: $\nu_0 = \frac{v}{2L}$ 

3. 1st overtone/2nd harmonics: $\nu_1 = 2\nu_0 = \frac{2v}{2L}$ 

4. 2nd overtone/3rd harmonics: $\nu_2 = 3\nu_0 = \frac{3v}{2L}$ 

5. All harmonics are present.

Resonance column:



$$l_1 + d = \frac{\lambda}{2}, \quad l_2 + d = \frac{3\lambda}{4}, \quad v = 2(l_2 - l_1)\nu$$

Beats: two waves of almost equal frequencies $\omega_1 \approx \omega_2$

$$p_1 = p_0 \sin \omega_1(t - x/v), \quad p_2 = p_0 \sin \omega_2(t - x/v)$$

$$p = p_1 + p_2 = 2p_0 \cos \Delta\omega(t - x/v) \sin \omega(t - x/v)$$

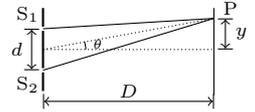
$$\omega = (\omega_1 + \omega_2)/2, \quad \Delta\omega = \omega_1 - \omega_2 \quad (\text{beats freq.})$$

Doppler Effect:

$$\nu = \frac{v + u_o}{v - u_s} \nu_0$$

where, v is the speed of sound in the medium, u_o is the speed of the observer w.r.t. the medium, considered positive when it moves towards the source and negative when it moves away from the source, and u_s is the speed of the source w.r.t. the medium, considered positive when it moves towards the observer and negative when it moves away from the observer.

Path difference: $\Delta x = \frac{dy}{D}$



Phase difference: $\delta = \frac{2\pi}{\lambda} \Delta x$

Interference Conditions: for integer n ,

$$\delta = \begin{cases} 2n\pi, & \text{constructive;} \\ (2n + 1)\pi, & \text{destructive,} \end{cases}$$

$$\Delta x = \begin{cases} n\lambda, & \text{constructive;} \\ (n + \frac{1}{2})\lambda, & \text{destructive} \end{cases}$$

Intensity:

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta,$$

$$I_{\max} = (\sqrt{I_1} + \sqrt{I_2})^2, \quad I_{\min} = (\sqrt{I_1} - \sqrt{I_2})^2$$

$$I_1 = I_2 : I = 4I_0 \cos^2 \frac{\delta}{2}, \quad I_{\max} = 4I_0, \quad I_{\min} = 0$$

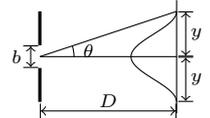
Fringe width: $w = \frac{\lambda D}{d}$

Optical path: $\Delta x' = \mu \Delta x$

Interference of waves transmitted through thin film:

$$\Delta x = 2\mu d = \begin{cases} n\lambda, & \text{constructive;} \\ (n + \frac{1}{2})\lambda, & \text{destructive.} \end{cases}$$

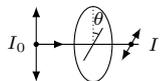
Diffraction from a single slit:



For Minima: $n\lambda = b \sin \theta \approx b(y/D)$

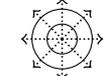
Resolution: $\sin \theta = \frac{1.22\lambda}{b}$

Law of Malus: $I = I_0 \cos^2 \theta$



2.4: Light Waves

Plane Wave: $E = E_0 \sin \omega(t - \frac{x}{v})$, $I = I_0$ 

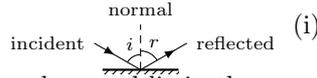
Spherical Wave: $E = \frac{aE_0}{r} \sin \omega(t - \frac{r}{v})$, $I = \frac{I_0}{r^2}$ 

Young's double slit experiment

Optics

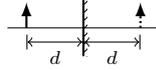
3.1: Reflection of Light

Laws of reflection:



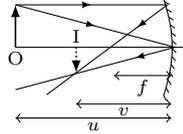
Incident ray, reflected ray, and normal lie in the same plane (ii) $\angle i = \angle r$

Plane mirror:



(i) the image and the object are equidistant from mirror (ii) virtual image of real object

Spherical Mirror:

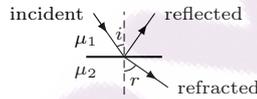


1. Focal length $f = R/2$
2. Mirror equation: $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$
3. Magnification: $m = -\frac{v}{u}$

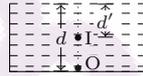
3.2: Refraction of Light

Refractive index: $\mu = \frac{\text{speed of light in vacuum}}{\text{speed of light in medium}} = \frac{c}{v}$

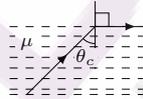
Snell's Law: $\frac{\sin i}{\sin r} = \frac{\mu_2}{\mu_1}$



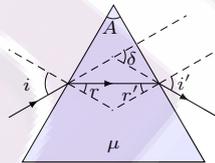
Apparent depth: $\mu = \frac{\text{real depth}}{\text{apparent depth}} = \frac{d}{d'}$



Critical angle: $\theta_c = \sin^{-1} \frac{1}{\mu}$



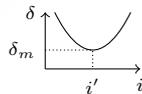
Deviation by a prism:



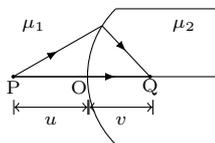
$\delta = i + i' - A$, general result

$\mu = \frac{\sin \frac{A + \delta_m}{2}}{\sin \frac{A}{2}}$, $i = i'$ for minimum deviation

$\delta_m = (\mu - 1)A$, for small A



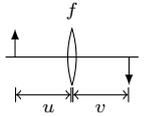
Refraction at spherical surface:



$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}, \quad m = \frac{\mu_1 v}{\mu_2 u}$$

Lens maker's formula: $\frac{1}{f} = (\mu - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$

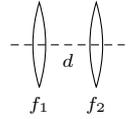
Lens formula: $\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$, $m = \frac{v}{u}$



Power of the lens: $P = \frac{1}{f}$, P in diopter if f in metre.

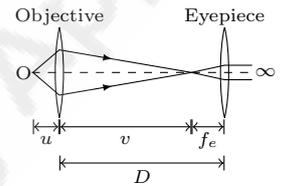
Two thin lenses separated by distance d:

$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2} - \frac{d}{f_1 f_2}$$



3.3: Optical Instruments

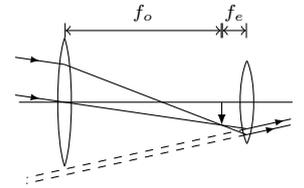
Simple microscope: $m = D/f$ in normal adjustment.



Compound microscope:

1. Magnification in normal adjustment: $m = \frac{v}{u} \frac{D}{f_e}$
2. Resolving power: $R = \frac{1}{\Delta d} = \frac{2\mu \sin \theta}{\lambda}$

Astronomical telescope:



1. In normal adjustment: $m = -\frac{f_o}{f_e}$, $L = f_o + f_e$
2. Resolving power: $R = \frac{1}{\Delta \theta} = \frac{1}{1.22 \lambda}$

3.4: Dispersion

Cauchy's equation: $\mu = \mu_0 + \frac{A}{\lambda^2}$, $A > 0$

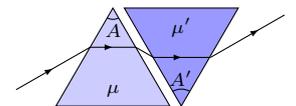
Dispersion by prism with small A and i:

1. Mean deviation: $\delta_y = (\mu_y - 1)A$
2. Angular dispersion: $\theta = (\mu_v - \mu_r)A$

Dispersive power: $\omega = \frac{\mu_v - \mu_r}{\mu_y - 1} \approx \frac{\theta}{\delta_y}$ (if A and i small)

Dispersion without deviation:

$$(\mu_y - 1)A + (\mu'_y - 1)A' = 0$$



Deviation without dispersion:

$$(\mu_v - \mu_r)A = (\mu'_v - \mu'_r)A'$$

Heat and Thermodynamics

4.1: Heat and Temperature

Temp. scales: $F = 32 + \frac{9}{5}C$, $K = C + 273.16$

Ideal gas equation: $pV = nRT$, n : number of moles

van der Waals equation: $(p + \frac{a}{V^2})(V - b) = nRT$

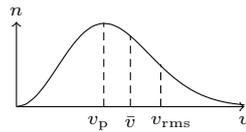
Thermal expansion: $L = L_0(1 + \alpha\Delta T)$,
 $A = A_0(1 + \beta\Delta T)$, $V = V_0(1 + \gamma\Delta T)$, $\gamma = 2\beta = 3\alpha$

Thermal stress of a material: $\frac{F}{A} = Y \frac{\Delta l}{l}$

4.2: Kinetic Theory of Gases

General: $M = mN_A$, $k = R/N_A$

Maxwell distribution of speed:



RMS speed: $v_{rms} = \sqrt{\frac{3kT}{m}} = \sqrt{\frac{3RT}{M}}$

Average speed: $\bar{v} = \sqrt{\frac{8kT}{\pi m}} = \sqrt{\frac{8RT}{\pi M}}$

Most probable speed: $v_p = \sqrt{\frac{2kT}{m}}$

Pressure: $p = \frac{1}{3}\rho v_{rms}^2$

Equipartition of energy: $K = \frac{1}{2}kT$ for each degree of freedom. Thus, $K = \frac{f}{2}kT$ for molecule having f degrees of freedoms.

Internal energy of n moles of an ideal gas is $U = \frac{f}{2}nRT$.

4.3: Specific Heat

Specific heat: $s = \frac{Q}{m\Delta T}$

Latent heat: $L = Q/m$

Specific heat at constant volume: $C_v = \left. \frac{\Delta Q}{n\Delta T} \right|_V$

Specific heat at constant pressure: $C_p = \left. \frac{\Delta Q}{n\Delta T} \right|_p$

Relation between C_p and C_v : $C_p - C_v = R$

Ratio of specific heats: $\gamma = C_p/C_v$

Relation between U and C_v : $\Delta U = nC_v\Delta T$

Specific heat of gas mixture:

$$C_v = \frac{n_1C_{v1} + n_2C_{v2}}{n_1 + n_2}, \quad \gamma = \frac{n_1C_{p1} + n_2C_{p2}}{n_1C_{v1} + n_2C_{v2}}$$

Molar internal energy of an ideal gas: $U = \frac{f}{2}RT$,
 $f = 3$ for monatomic and $f = 5$ for diatomic gas.

4.4: Thermodynamic Processes

First law of thermodynamics: $\Delta Q = \Delta U + \Delta W$

Work done by the gas:

$$\Delta W = p\Delta V, \quad W = \int_{V_1}^{V_2} pdV$$

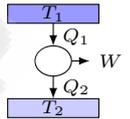
$$W_{\text{isothermal}} = nRT \ln \left(\frac{V_2}{V_1} \right)$$

$$W_{\text{isobaric}} = p(V_2 - V_1)$$

$$W_{\text{adiabatic}} = \frac{p_1V_1 - p_2V_2}{\gamma - 1}$$

$$W_{\text{isochoric}} = 0$$

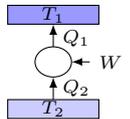
Efficiency of the heat engine:



$$\eta = \frac{\text{work done by the engine}}{\text{heat supplied to it}} = \frac{Q_1 - Q_2}{Q_1}$$

$$\eta_{\text{carnot}} = 1 - \frac{Q_2}{Q_1} = 1 - \frac{T_2}{T_1}$$

Coeff. of performance of refrigerator:



$$\text{COP} = \frac{Q_2}{W} = \frac{Q_2}{Q_1 - Q_2}$$

Entropy: $\Delta S = \frac{\Delta Q}{T}$, $S_f - S_i = \int_i^f \frac{\Delta Q}{T}$

$$\text{Const. } T : \Delta S = \frac{Q}{T}, \quad \text{Varying } T : \Delta S = ms \ln \frac{T_f}{T_i}$$

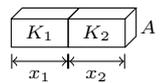
Adiabatic process: $\Delta Q = 0$, $pV^\gamma = \text{constant}$

4.5: Heat Transfer

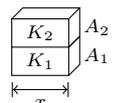
Conduction: $\frac{\Delta Q}{\Delta t} = -KA \frac{\Delta T}{x}$

Thermal resistance: $R = \frac{x}{KA}$

$$R_{\text{series}} = R_1 + R_2 = \frac{1}{A} \left(\frac{x_1}{K_1} + \frac{x_2}{K_2} \right)$$

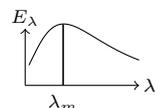


$$\frac{1}{R_{\text{parallel}}} = \frac{1}{R_1} + \frac{1}{R_2} = \frac{1}{x} (K_1A_1 + K_2A_2)$$



Kirchhoff's Law: $\frac{\text{emissive power}}{\text{absorptive power}} = \frac{E_{\text{body}}}{a_{\text{body}}} = E_{\text{blackbody}}$

Wien's displacement law: $\lambda_m T = b$



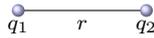
Stefan-Boltzmann law: $\frac{\Delta Q}{\Delta t} = \sigma eAT^4$

Newton's law of cooling: $\frac{dT}{dt} = -bA(T - T_0)$

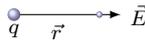
Electricity and Magnetism

5.1: Electrostatics

Coulomb's law: $\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{r}$



Electric field: $\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$

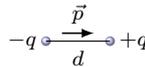


Electrostatic energy: $U = -\frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$

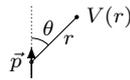
Electrostatic potential: $V = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$

$$dV = -\vec{E} \cdot d\vec{r}, \quad V(\vec{r}) = -\int_{\infty}^{\vec{r}} \vec{E} \cdot d\vec{r}$$

Electric dipole moment: $\vec{p} = q\vec{d}$

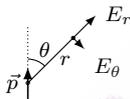


Potential of a dipole: $V = \frac{1}{4\pi\epsilon_0} \frac{p \cos \theta}{r^2}$



Field of a dipole:

$$E_r = \frac{1}{4\pi\epsilon_0} \frac{2p \cos \theta}{r^3}, \quad E_\theta = \frac{1}{4\pi\epsilon_0} \frac{p \sin \theta}{r^3}$$



Torque on a dipole placed in \vec{E} : $\vec{\tau} = \vec{p} \times \vec{E}$

Pot. energy of a dipole placed in \vec{E} : $U = -\vec{p} \cdot \vec{E}$

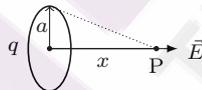
5.2: Gauss's Law and its Applications

Electric flux: $\phi = \oint \vec{E} \cdot d\vec{S}$

Gauss's law: $\oint \vec{E} \cdot d\vec{S} = q_{in}/\epsilon_0$

Field of a uniformly charged ring on its axis:

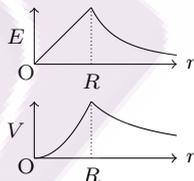
$$E_P = \frac{1}{4\pi\epsilon_0} \frac{qx}{(a^2+x^2)^{3/2}}$$



E and V of a uniformly charged sphere:

$$E = \begin{cases} \frac{1}{4\pi\epsilon_0} \frac{Qr}{R^3}, & \text{for } r < R \\ \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}, & \text{for } r \geq R \end{cases}$$

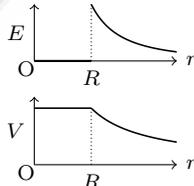
$$V = \begin{cases} \frac{1}{4\pi\epsilon_0} \frac{Qr^2}{2R^3}, & \text{for } r < R \\ \frac{1}{4\pi\epsilon_0} \frac{Q}{r}, & \text{for } r \geq R \end{cases}$$



E and V of a uniformly charged spherical shell:

$$E = \begin{cases} 0, & \text{for } r < R \\ \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}, & \text{for } r \geq R \end{cases}$$

$$V = \begin{cases} \frac{1}{4\pi\epsilon_0} \frac{Q}{R}, & \text{for } r < R \\ \frac{1}{4\pi\epsilon_0} \frac{Q}{r}, & \text{for } r \geq R \end{cases}$$



Field of a line charge: $E = \frac{\lambda}{2\pi\epsilon_0 r}$

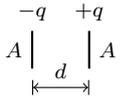
Field of an infinite sheet: $E = \frac{\sigma}{2\epsilon_0}$

Field in the vicinity of conducting surface: $E = \frac{\sigma}{\epsilon_0}$

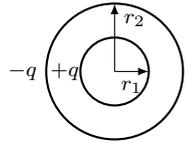
5.3: Capacitors

Capacitance: $C = q/V$

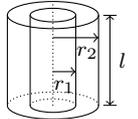
Parallel plate capacitor: $C = \epsilon_0 A/d$



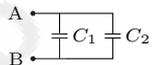
Spherical capacitor: $C = \frac{4\pi\epsilon_0 r_1 r_2}{r_2 - r_1}$



Cylindrical capacitor: $C = \frac{2\pi\epsilon_0 l}{\ln(r_2/r_1)}$



Capacitors in parallel: $C_{eq} = C_1 + C_2$



Capacitors in series: $\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$



Force between plates of a parallel plate capacitor:

$$F = \frac{Q^2}{2A\epsilon_0}$$

Energy stored in capacitor: $U = \frac{1}{2} CV^2 = \frac{Q^2}{2C} = \frac{1}{2} QV$

Energy density in electric field E: $U/V = \frac{1}{2} \epsilon_0 E^2$

Capacitor with dielectric: $C = \frac{\epsilon_0 K A}{d}$

5.4: Current electricity

Current density: $j = i/A = \sigma E$

Drift speed: $v_d = \frac{1}{2} \frac{eE}{m} \tau = \frac{i}{neA}$

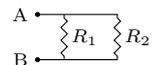
Resistance of a wire: $R = \rho l/A$, where $\rho = 1/\sigma$

Temp. dependence of resistance: $R = R_0(1 + \alpha \Delta T)$

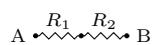
Ohm's law: $V = iR$

Kirchhoff's Laws: (i) *The Junction Law:* The algebraic sum of all the currents directed towards a node is zero i.e., $\sum_{\text{node}} I_i = 0$. (ii) *The Loop Law:* The algebraic sum of all the potential differences along a closed loop in a circuit is zero i.e., $\sum_{\text{loop}} \Delta V_i = 0$.

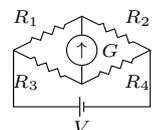
Resistors in parallel: $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$



Resistors in series: $R_{eq} = R_1 + R_2$



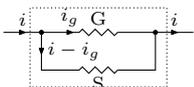
Wheatstone bridge:



Balanced if $R_1/R_2 = R_3/R_4$.

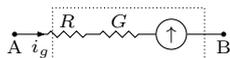
Electric Power: $P = V^2/R = I^2 R = IV$

Galvanometer as an Ammeter:



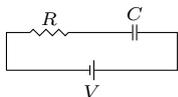
$$i_g G = (i - i_g) S$$

Galvanometer as a Voltmeter:



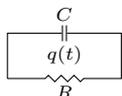
$$V_{AB} = i_g (R + G)$$

Charging of capacitors:



$$q(t) = CV \left[1 - e^{-\frac{t}{RC}} \right]$$

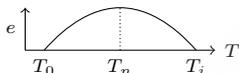
Discharging of capacitors: $q(t) = q_0 e^{-\frac{t}{RC}}$



Time constant in RC circuit: $\tau = RC$

Peltier effect: $\text{emf } e = \frac{\Delta H}{\Delta Q} = \frac{\text{Peltier heat}}{\text{charge transferred}}$

Seebeck effect:



1. Thermo-emf: $e = aT + \frac{1}{2}bT^2$
2. Thermoelectric power: $de/dt = a + bT$.
3. Neutral temp.: $T_n = -a/b$.
4. Inversion temp.: $T_i = -2a/b$.

Thomson effect: $\text{emf } e = \frac{\Delta H}{\Delta Q} = \frac{\text{Thomson heat}}{\text{charge transferred}} = \sigma \Delta T$.

Faraday's law of electrolysis: The mass deposited is

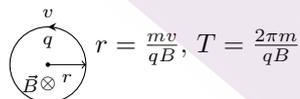
$$m = Zit = \frac{1}{F} Eit$$

where i is current, t is time, Z is electrochemical equivalent, E is chemical equivalent, and $F = 96485 \text{ C/g}$ is Faraday constant.

5.5: Magnetism

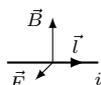
Lorentz force on a moving charge: $\vec{F} = q\vec{v} \times \vec{B} + q\vec{E}$

Charged particle in a uniform magnetic field:



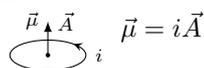
$$r = \frac{mv}{qB}, T = \frac{2\pi m}{qB}$$

Force on a current carrying wire:



$$\vec{F} = i \vec{l} \times \vec{B}$$

Magnetic moment of a current loop (dipole):



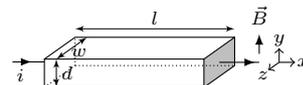
$$\vec{\mu} = i\vec{A}$$

Torque on a magnetic dipole placed in B: $\vec{\tau} = \vec{\mu} \times \vec{B}$

Energy of a magnetic dipole placed in B:

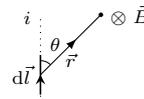
$$U = -\vec{\mu} \cdot \vec{B}$$

Hall effect: $V_w = \frac{Bi}{ned}$

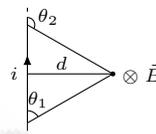


5.6: Magnetic Field due to Current

Biot-Savart law: $d\vec{B} = \frac{\mu_0}{4\pi} \frac{i d\vec{l} \times \vec{r}}{r^3}$



Field due to a straight conductor:



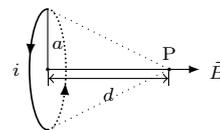
$$B = \frac{\mu_0 i}{4\pi d} (\cos \theta_1 - \cos \theta_2)$$

Field due to an infinite straight wire: $B = \frac{\mu_0 i}{2\pi d}$

Force between parallel wires: $\frac{dF}{dl} = \frac{\mu_0 i_1 i_2}{2\pi d}$

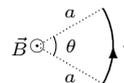


Field on the axis of a ring:



$$B_P = \frac{\mu_0 i a^2}{2(a^2 + d^2)^{3/2}}$$

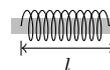
Field at the centre of an arc: $B = \frac{\mu_0 i \theta}{4\pi a}$



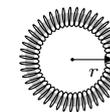
Field at the centre of a ring: $B = \frac{\mu_0 i}{2a}$

Ampere's law: $\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{in}$

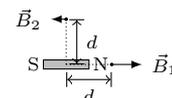
Field inside a solenoid: $B = \mu_0 n i$, $n = \frac{N}{l}$



Field inside a toroid: $B = \frac{\mu_0 N i}{2\pi r}$

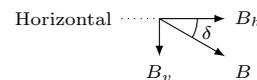


Field of a bar magnet:



$$B_1 = \frac{\mu_0}{4\pi} \frac{2M}{d^3}, \quad B_2 = \frac{\mu_0}{4\pi} \frac{M}{d^3}$$

Angle of dip: $B_h = B \cos \delta$



Tangent galvanometer: $B_h \tan \theta = \frac{\mu_0 n i}{2r}$, $i = K \tan \theta$

Moving coil galvanometer: $n i A B = k\theta$, $i = \frac{k}{nAB} \theta$

Time period of magnetometer: $T = 2\pi \sqrt{\frac{I}{MB_h}}$

Permeability: $\vec{B} = \mu \vec{H}$

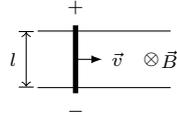
5.7: Electromagnetic Induction

Magnetic flux: $\phi = \oint \vec{B} \cdot d\vec{S}$

Faraday's law: $e = -\frac{d\phi}{dt}$

Lenz's Law: Induced current create a B -field that opposes the change in magnetic flux.

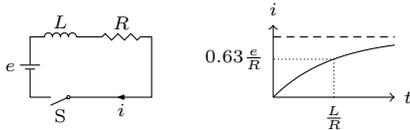
Motional emf: $e = Blv$



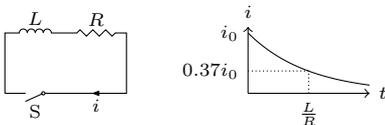
Self inductance: $\phi = Li$, $e = -L\frac{di}{dt}$

Self inductance of a solenoid: $L = \mu_0 n^2 (\pi r^2 l)$

Growth of current in LR circuit: $i = \frac{e}{R} [1 - e^{-\frac{t}{L/R}}]$



Decay of current in LR circuit: $i = i_0 e^{-\frac{t}{L/R}}$



Time constant of LR circuit: $\tau = L/R$

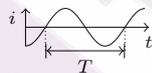
Energy stored in an inductor: $U = \frac{1}{2} Li^2$

Energy density of B field: $u = \frac{U}{V} = \frac{B^2}{2\mu_0}$

Mutual inductance: $\phi = Mi$, $e = -M\frac{di}{dt}$

EMF induced in a rotating coil: $e = NAB\omega \sin \omega t$

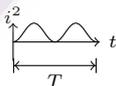
Alternating current:



$$i = i_0 \sin(\omega t + \phi), \quad T = 2\pi/\omega$$

Average current in AC: $\bar{i} = \frac{1}{T} \int_0^T i dt = 0$

RMS current: $i_{\text{rms}} = \left[\frac{1}{T} \int_0^T i^2 dt \right]^{1/2} = \frac{i_0}{\sqrt{2}}$



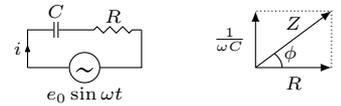
Energy: $E = i_{\text{rms}}^2 RT$

Capacitive reactance: $X_c = \frac{1}{\omega C}$

Inductive reactance: $X_L = \omega L$

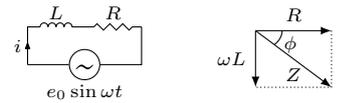
Impedance: $Z = e_0/i_0$

RC circuit:



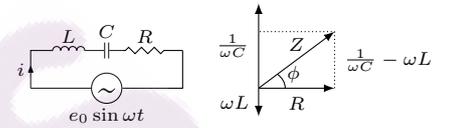
$$Z = \sqrt{R^2 + (1/\omega C)^2}, \quad \tan \phi = \frac{1}{\omega C R}$$

LR circuit:



$$Z = \sqrt{R^2 + \omega^2 L^2}, \quad \tan \phi = \frac{\omega L}{R}$$

LCR Circuit:

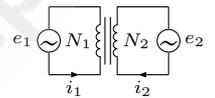


$$Z = \sqrt{R^2 + \left(\frac{1}{\omega C} - \omega L\right)^2}, \quad \tan \phi = \frac{\frac{1}{\omega C} - \omega L}{R}$$

$$\nu_{\text{resonance}} = \frac{1}{2\pi} \sqrt{\frac{1}{LC}}$$

Power factor: $P = e_{\text{rms}} i_{\text{rms}} \cos \phi$

Transformer: $\frac{N_1}{N_2} = \frac{e_1}{e_2}$, $e_1 i_1 = e_2 i_2$



Speed of the EM waves in vacuum: $c = 1/\sqrt{\mu_0 \epsilon_0}$

Modern Physics

6.1: Photo-electric effect

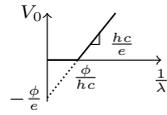
Photon's energy: $E = h\nu = hc/\lambda$

Photon's momentum: $p = h/\lambda = E/c$

Max. KE of ejected photo-electron: $K_{\max} = h\nu - \phi$

Threshold freq. in photo-electric effect: $\nu_0 = \phi/h$

Stopping potential: $V_o = \frac{hc}{e} \left(\frac{1}{\lambda}\right) - \frac{\phi}{e}$



de Broglie wavelength: $\lambda = h/p$

6.2: The Atom

Energy in n th Bohr's orbit:

$$E_n = -\frac{mZ^2e^4}{8\epsilon_0^2h^2n^2}, \quad E_n = -\frac{13.6Z^2}{n^2} \text{ eV}$$

Radius of the n th Bohr's orbit:

$$r_n = \frac{\epsilon_0h^2n^2}{\pi mZe^2}, \quad r_n = \frac{n^2a_0}{Z}, \quad a_0 = 0.529 \text{ \AA}$$

Quantization of the angular momentum: $l = \frac{nh}{2\pi}$

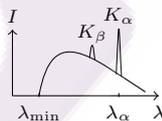
Photon energy in state transition: $E_2 - E_1 = h\nu$



Wavelength of emitted radiation: for a transition from n th to m th state:

$$\frac{1}{\lambda} = RZ^2 \left[\frac{1}{n^2} - \frac{1}{m^2} \right]$$

X-ray spectrum: $\lambda_{\min} = \frac{hc}{eV}$



Moseley's law: $\sqrt{\nu} = a(Z - b)$

X-ray diffraction: $2d \sin \theta = n\lambda$

Heisenberg uncertainty principle:

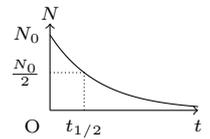
$$\Delta p \Delta x \geq h/(2\pi), \quad \Delta E \Delta t \geq h/(2\pi)$$

6.3: The Nucleus

Nuclear radius: $R = R_0A^{1/3}$, $R_0 \approx 1.1 \times 10^{-15} \text{ m}$

Decay rate: $\frac{dN}{dt} = -\lambda N$

Population at time t : $N = N_0e^{-\lambda t}$



Half life: $t_{1/2} = 0.693/\lambda$

Average life: $t_{av} = 1/\lambda$

Population after n half lives: $N = N_0/2^n$

Mass defect: $\Delta m = [Zm_p + (A - Z)m_n] - M$

Binding energy: $B = [Zm_p + (A - Z)m_n - M] c^2$

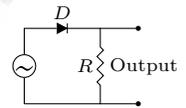
Q-value: $Q = U_i - U_f$

Energy released in nuclear reaction: $\Delta E = \Delta mc^2$

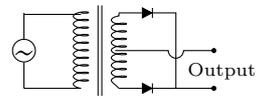
where $\Delta m = m_{\text{reactants}} - m_{\text{products}}$

6.4: Vacuum tubes and Semiconductors

Half Wave Rectifier:



Full Wave Rectifier:



Triode Valve:

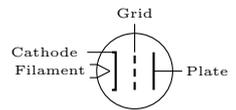


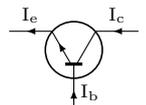
Plate resistance of a triode: $r_p = \left. \frac{\Delta V_p}{\Delta i_p} \right|_{\Delta V_g=0}$

Transconductance of a triode: $g_m = \left. \frac{\Delta i_p}{\Delta V_g} \right|_{\Delta V_p=0}$

Amplification by a triode: $\mu = - \left. \frac{\Delta V_p}{\Delta V_g} \right|_{\Delta i_p=0}$

Relation between r_p , μ , and g_m : $\mu = r_p \times g_m$

Current in a transistor: $I_e = I_b + I_c$



α and β parameters of a transistor: $\alpha = \frac{I_c}{I_e}$, $\beta = \frac{I_c}{I_b}$

Transconductance: $g_m = \frac{\Delta I_c}{\Delta V_{be}}$

Logic Gates:

		AND	OR	NAND	NOR	XOR
A	B	AB	A+B	\overline{AB}	$\overline{A+B}$	$A\overline{B} + \overline{A}B$
0	0	0	0	1	1	0
0	1	0	1	1	0	1
1	0	0	1	1	0	1
1	1	1	1	0	0	0